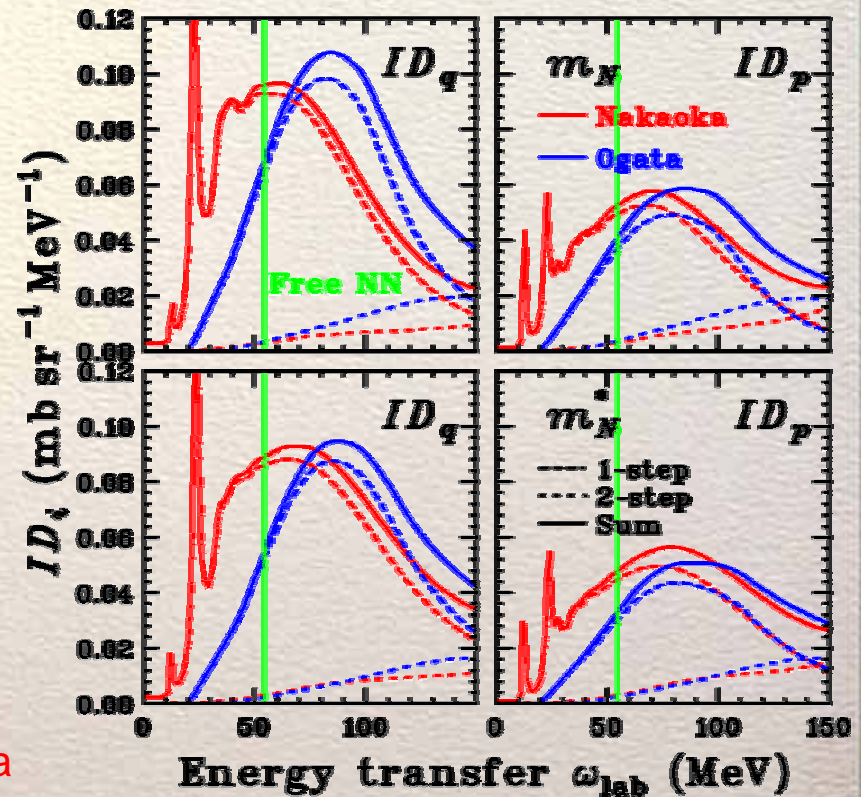


# Comparison between theoretical calculations for QES processes

- Nakaoka et al.
  - PWA for 2-step; DWIA+free for 1-step
  - Franey and Love t-matrix
  - Free-mass case: On-shell approx.
  - $m^*$  case: w/o on-shell approx.
- Ogata et al.
  - SCDW model
  - Melbourne free t-matrix
  - Free-mass and  $m^*$  cases
- Results
  - Free-mass:  $m$ 
    - 1-step: Nakaoka    Ogata
    - 2-step: Nakaoka < Ogata
  - Effective mass:  $m^*$ 
    - 1- and 2-steps: Nakaoka    Ogata
  - Peak shift from free NN
    - Nakaoka: little shift (*energy dependence of distortion effects*)
    - Ogata: large shift



# Peak shift mechanism and binding-energy effect for QES

- Energy transfer  $\omega$  for QES at  $q$

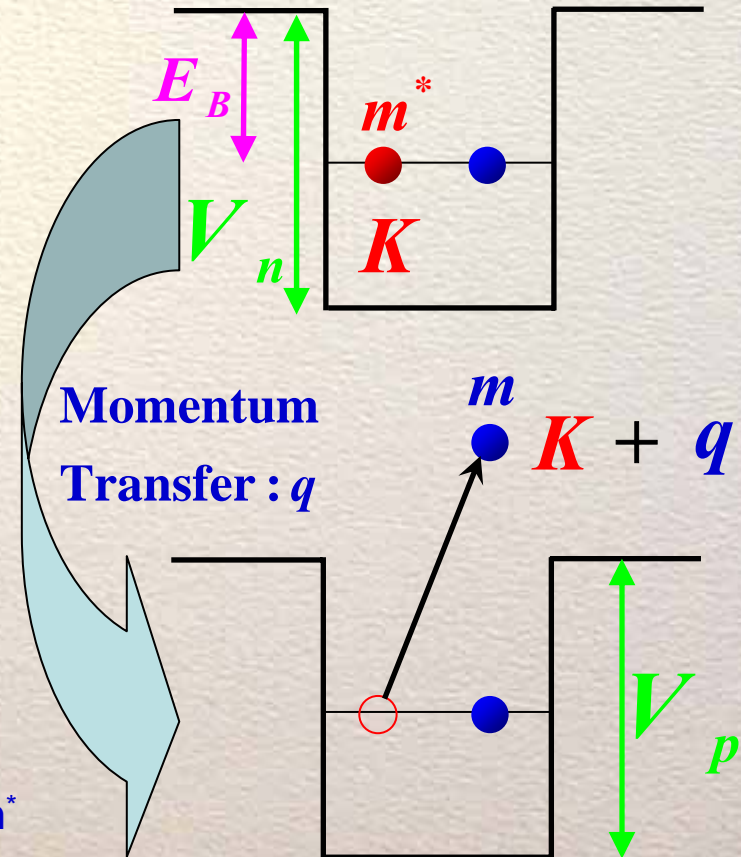
$$\omega = \left[ \frac{(K+q)^2}{2m} + V_p \right] - \left[ \frac{K^2}{2m} + V_n \right]$$

$$= \frac{q^2}{2m} + \frac{K \cdot q}{m}$$

↑ NN Peak    
 ↑ Width    
 ↓ Peak Shift

$$+ \frac{K^2}{2} \left( \frac{1}{m} - \frac{1}{m^*} \right) + (V_p - V_n)$$

- Binding energy  $E_B$  does not contribute to the peak shift
- Peak shift depends on single particle potentials  $V$  and the effective mass  $m^*$
- (p,n): Shift = 20-30 MeV
- (p,p'): Shift = 0-10 MeV



# Peak shift mechanism and Q-value effect for QES

- $^{12}\text{C}(p,n)$  case

Single particle	Energy (B.E.)	Potential
Neutron in $^{12}\text{C}$	$B_n = -18.72 \text{ MeV}$	$V_n = -72.76 \text{ MeV}$
Proton in $^{12}\text{N}$	$B_p = -0.60 \text{ MeV}$	$V_p = -49.92 \text{ MeV}$

- $Q = B_n - B_p = -18.1 \text{ MeV} \approx \Delta V = V_n - V_p = -22.8 \text{ MeV}$
- **Shell Gap**  $\ll Q \approx \Delta V \approx \Delta\omega$

- $^{40}\text{Ca}(p,n)$  case

Single particle	Energy (B.E.)	Potential
Neutron in $^{40}\text{Ca}$	$B_n = -15.64 \text{ MeV}$	$V_n = -64.42 \text{ MeV}$
Proton in $^{40}\text{Sc}$	$B_p = -0.54 \text{ MeV}$	$V_p = -60.63 \text{ MeV}$

- $Q = B_n - B_p = -15.1 \text{ MeV} \ll \Delta V = V_n - V_p = -3.8 \text{ MeV}$
- **Shell Gap**  $\approx Q \approx \Delta\omega \ll \Delta V$

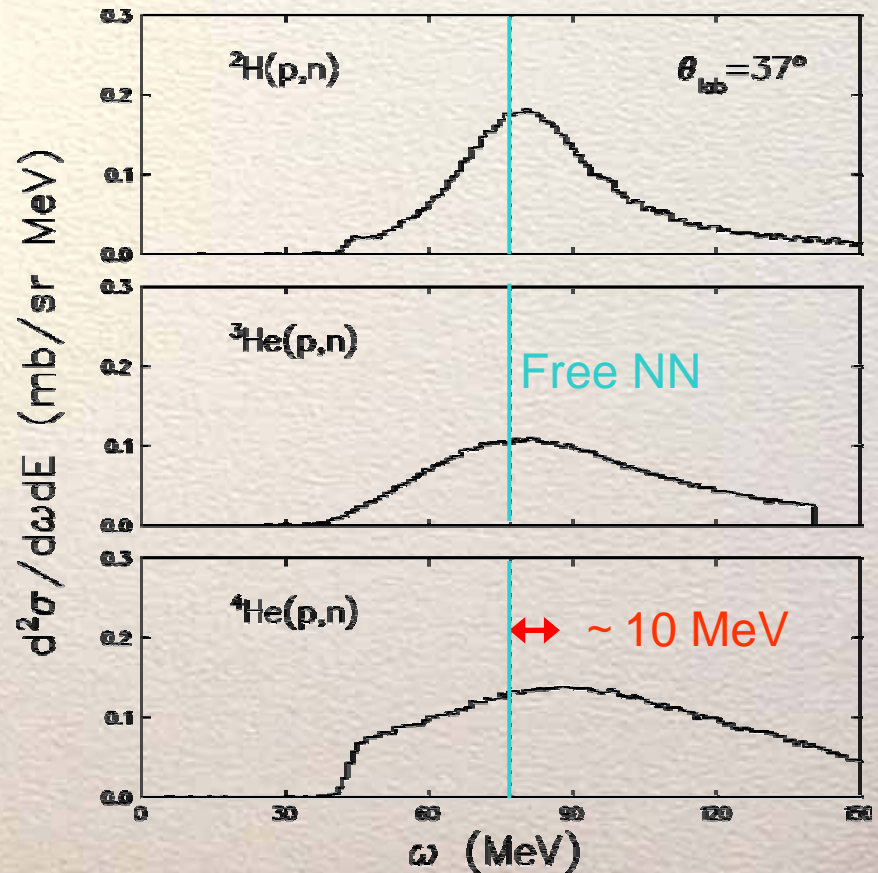
- QES peak shift:  $\sim 20 \text{ MeV}$  for  $^{12}\text{C}(p,n)$  and  $^{40}\text{Ca}(p,n)$

- should depend on  $V$
- $V$  **X**  $Q$  **X**  $Q$

QES peak should not (directly) depend on Q-value

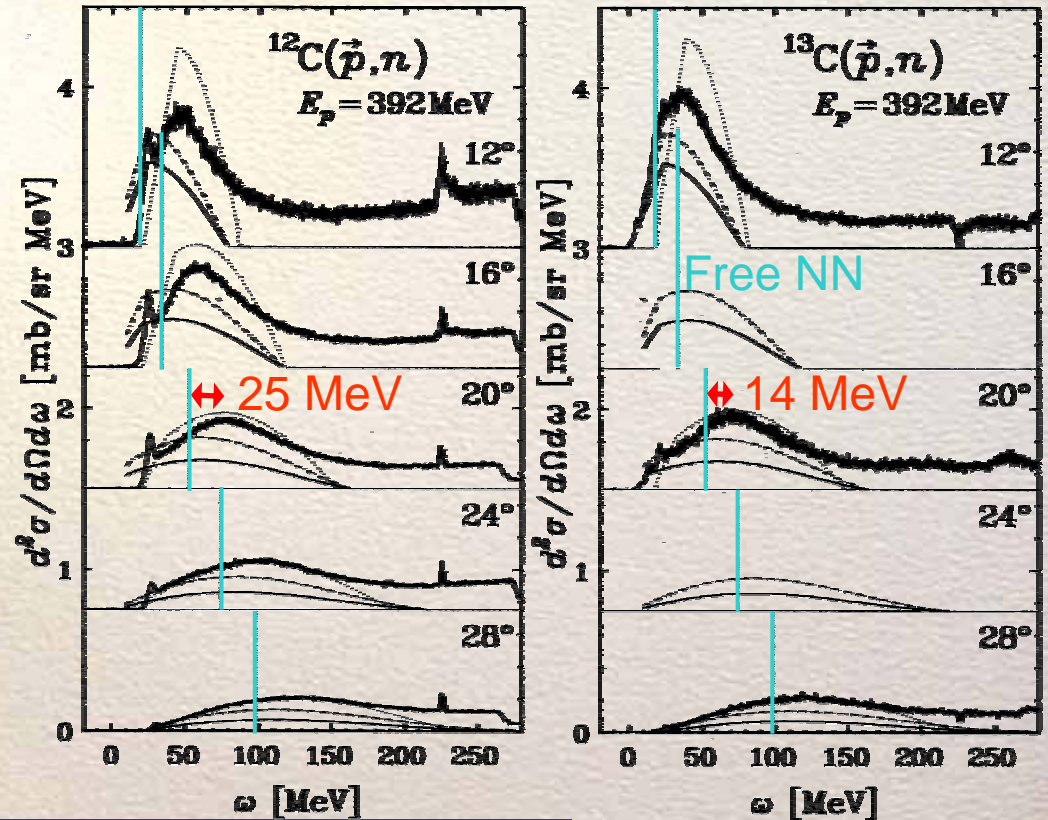
# QES peak shift for light nuclei

- $^2\text{H}$ ,  $^3\text{He}(p,n)$ 
  - Q-values
    - $^2\text{H}$ : -2.2 MeV (Break-up)
    - $^3\text{He}$ : -1.8 MeV
  - Almost no shift
  - $m^*$  and  $\Delta V$  effects: ✘
- $^4\text{He}(p,n)$ 
  - Q-value: -23.7 MeV
  - Peak shift:  $\sim 10$  MeV  
 $< Q$ -value
  - $m^*$  and  $\Delta V$  effects ?



# QES peak shift for C isotopes

- $^{12}\text{C}, ^{13}\text{C}(p,n)$ 
  - $m^*$  and distortion effects would be same
  - Q-values
    - $^{12}\text{C}$ : -18.1 MeV
    - $^{13}\text{C}$ : -3.0 MeV
  - Single particle potential
    - $^{12}\text{C}$ :  $\Delta V=22.8$  MeV
    - $^{13}\text{C}$ :  $\Delta V= 0.5$  MeV
  - Peak shift
    - $^{12}\text{C}$ :  $\Delta\omega=25 \pm 3$  MeV
    - $^{13}\text{C}$ :  $\Delta\omega=14 \pm 7$  MeV



- Results
  - Peak-shift difference  $\sim$  Q-value difference
  - Peak-shift difference  $<$   $\Delta V$  difference
  - $\Delta V$  difference for C isotopes is physically appropriate?

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Doctoral Dissertation  
Univ. of Tokyo (1997)*

# Distortion, $m^*$ , and correlation effects for QES peak shift

- PWIA/DWIA calculations
  - PW vs. DW
  - $m$  (free mass) vs.  $m^*$  (effective mass)
  - Free response ( $0^{\text{th}}$ ) vs. RPA response
- Contribution to peak shift
  - PW+m+Free response( $0^{\text{th}}$ ) = Free NN
  - Distortion: +8 MeV
  - $m^*$ (effective mass): +6 MeV
  - RPA (correlation): +6 MeV
  - Total: +20 MeV

